



De Silva, G., Burgess, S. C., Hatano, T., Khan, S. G., Zhang, K., Nguyen, T., Herrmann, G., Edwards, C., & Miles, M. (2017). Optimisation of a nano-positioning stage for a Transverse Dynamic Force Microscope. *Precision Engineering - Journal of the International Societies for Precision Engineering and Nanotechnology*, 50, 183-197. [1]. <https://doi.org/10.1016/j.precisioneng.2017.05.005>

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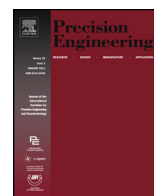
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## Research paper

# Optimisation of a nano-positioning stage for a Transverse Dynamic Force Microscope



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## ARTICLE INFO

## Article history:

Received 12 July 2016

Received in revised form

19 December 2016

Accepted 4 May 2017

Available online 10 May 2017

## Keywords:

Design optimisation

Prototype testing

Fea

Atomic force microscope

## ABSTRACT

This paper describes the optimisation of a nano-positioning stage for a Transverse Dynamic Force Microscope (TDFM). The nano-precision stage is required to move a specimen dish within a horizontal region of  $1\ \mu\text{m} \times 1\ \mu\text{m}$  and with a resolution of 0.3 nm. The design objective was to maximise positional accuracy during high speed actuation. This was achieved by minimising out-of-plane distortions and vibrations during actuation. Optimal performance was achieved through maximising out-of-plane stiffness through shape and material selection as well optimisation of the anchoring system. Several shape parameters were optimised including the shape of flexural beams and the shape of the dish holder. Physical prototype testing was an essential part of the design process to confirm the accuracy of modelling and also to reveal issues with manufacturing tolerances. An overall resonant frequency of 6 kHz was achieved allowing for a closed loop-control frequency of 1.73 kHz for precise horizontal motion control. This resonance represented a 12-fold increase from the original 500 Hz of a commercially available positioning stage. Experimental maximum out-of-plane distortions below the first resonance frequency were reduced from  $0.3\ \mu\text{m}$  for the first prototype to less than  $0.05\ \mu\text{m}$  for the final practical prototype.

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## 1. Introduction

### 1.1. The need for design optimisation of atomic force microscopes

Since its invention in 1986 [1], atomic force microscopes (AFMs) have become one of the most important tools to measure the 3-D topography of nano-scale objects including both biological and non-biological specimens [2–4]. The resolution of AFMs can be better than 1 nanometre ( $1 \times 10^{-9}\ \text{m}$ ) enabling measurements of specimens such as DNA and proteins [5]. AFMs are widely used for biomedical analysis in cancer research [6], cell biology research [7] and material science [8].

AFMs have a number of advantages over scanning electron microscopes (SEMs) such as the ability to carry out 3D scanning, the ability to scan untreated specimens and the ability to scan without the need for a vacuum. However one of the key disadvantages of AFMs is relatively slow scanning rates. This is restricting the use-

fulness of AFMs in many areas of research. In particular AFMs are generally not able to scan processes in real time.

This paper deals with the optimisation of the positioning stage of an advanced type of atomic force microscope called a transverse dynamic atomic force microscope (TDFM). A TDFM has higher accuracy and the capability to scan softer specimens [9]. However, as with other types of AFM, TDFMs suffer from slow scan rates. In addition their resolution can be limited when scanning rates are high. Therefore there is a need for design optimisation of TDFMs to achieve improved levels of resolution and speed of scanning. In particular, the positioning stage, which moves the sample under the probe, is a critical component that limits the speed and accuracy of operation.

### 1.2. Introduction to the transverse dynamic force microscope

The basic layout of a TDFM is shown in Fig. 1. The specimen to be examined is placed on a thin specimen dish within a nano-positioning stage that can be moved in a horizontal x-y plane. Conditions must be such that the specimen is covered with a microscopic water layer as this is required for the scanning process. In ambient conditions, a specimen is always covered with a thin water

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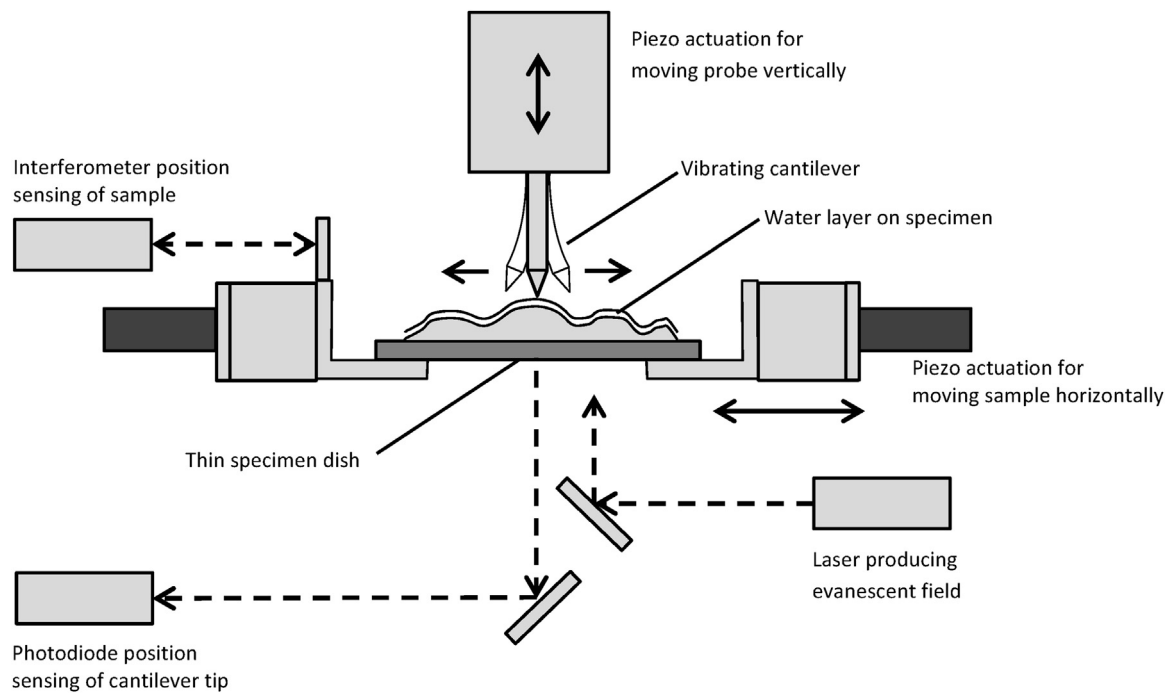


Fig. 1. Schematic of the TDFM layout.

layer due to general humidity at room temperature and pressure (21 °C, 100 kPa).

A TDFM uses a vertically orientated cantilever probe which is different to the horizontally orientated probes of traditional AFMs [9–13]. The vertical cantilever is vibrated at a set frequency and placed above the specimen in close proximity such that there is interaction between the cantilever and the molecules of water within the microscopic water layer that covers the specimen.

When the cantilever interacts with the water layer the vibration is damped and the amplitude of vibration is decreased. The exact amplitude of vibration is dependent on the level of penetration in the water layer. During scanning, if the probe is moved in the vertical axis such that the amplitude of vibration is constant then the probe follows the profile of the specimen. This principle of interaction with the water layer above the specimen enables non-contact scanning.

The change in vibration of the probe is measured by a laser optical detection system, which is set beneath the thin specimen dish underneath the specimen. The optical detection system creates scattered evanescent electromagnetic waves in the surrounding area of the specimen [14]. The reflected component of these is detected by a photo-detection system to obtain a measurement of the cantilever tip oscillation.

### 1.3. Introduction to the nano-positioning system

The layout of the positioning stage is shown in Fig. 2a and is based on a concept produced by Schitter et al., 2006 [15]. The nano-positioning stage consists of:

- A structural element.
- A central circular specimen dish.
- Four piezo actuators.
- Four side clamps.
- Two mirrors.

The structural element itself consists of a number of separate features including four primary flexural beams; twelve secondary

flexural beams; a central dish holder, two mirror holders; and four anchor points.

The primary beams are deflected directly by the adjacent piezo actuator as shown in Fig. 2b and allow a deflection of 1  $\mu\text{m}$  in the x and z axes. The secondary beams allow simultaneous movement of the dish in x and y directions. The combination of primary and secondary beams give the required stiffness.

Piezoelectric actuators are used because of their high stiffness, linear displacement and high load capacity. A laser-interferometer system is used to detect movement in the x and y axes, as it gives a high positioning accuracy of 0.3 nm.

There are two vertical mounts (flags), one on each axis, protruding from the edge of the specimen holder. They are used for the attachment of thin mirrors, acting as reflectors for the two laser beams of the laser interferometer. The 'T shaped' side clamps are used to apply/adjust the mechanical preload applied to the piezo actuators.

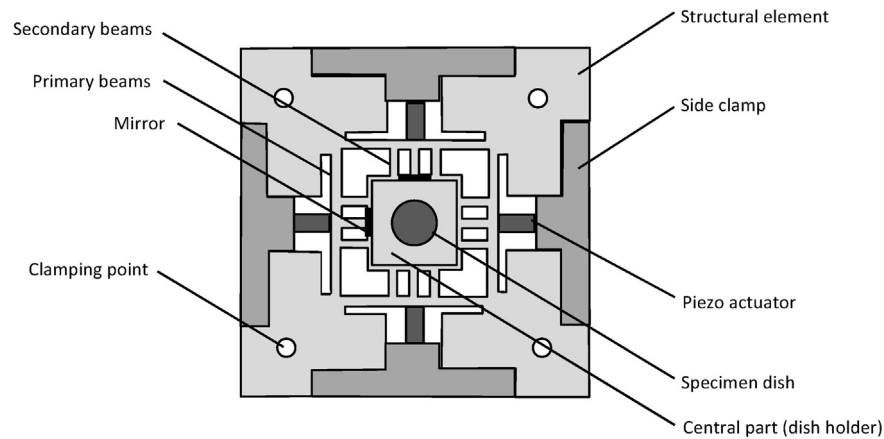
### 1.4. Performance of TDFMs

The main measures of technical performance are scan accuracy and speed. These are very closely linked to two physical properties: (i) the natural frequency of positioning stage and (ii) the out-of-plane distortions of the stage during in-plane movement. Higher natural frequencies result in a higher bandwidth and hence scan rates. Low out-of-plane distortions mean that the accuracy is better for both stage position measurement and probe position measurement.

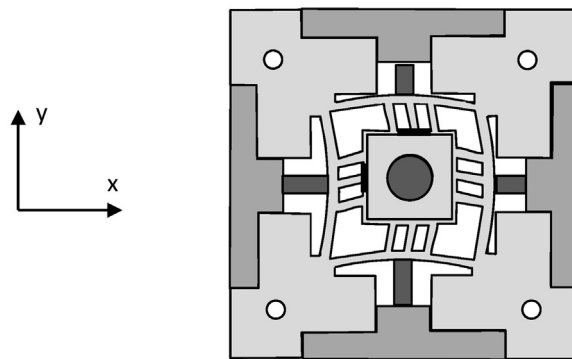
### 1.5. Design constraints and objectives

The positioning system has the following constraints and requirements:

- The design space for the structural element is 93 mm  $\times$  93 mm  $\times$  9 mm.
- The dish holder must be able to displace up to 1  $\mu\text{m}$  in the x and y axes.



(a) Layout of positioning stage



(b) Example of x and y movement of the dish holder via flexing of structural beams

**Fig. 2.** Assembly of the positioning stage.

- The stage must hold a specimen holder disc of 18 mm diameter.
- The design space for the specimen dish is shown in Fig. 3.

The overall design objectives for the nano-positioning stage are:

- lowest natural frequency >6000 Hz.
- experimental out-of-plane displacements <0.05  $\mu\text{m}$  (for 1  $\mu\text{m}$  x and y in-plane movement; corresponds to a –25 dB gain for out-of-plane to in-plane displacement.).

#### 1.6. Current performance of TDFMs

For the first prototype we used the high precision stage of the Physik Instrumente, P-733.2, [16]. This had a minimum resonance of 500 Hz which limited the bandwidth of any motion to less than 300 Hz, although account should be taken that it has a relatively large motion range of 100  $\mu\text{m}$ . Other commercial precision stages for this purpose have at best resonance frequencies at about 2000 Hz [17]. Therefore significant design optimisation was required to meet the design goals.

## 2. Conceptual design of a new positioning stage

### 2.1. Existing designs

Some of the main types of positioning stage geometries are shown in Table 1. An example of the comb-flexure concept is given

by Schitter et al. [15] and involves direct and symmetric loading. An example of a hybrid flexure is given by Yong et al. [18] and involves indirect loading but a symmetric flexure layout. An example of a stage with direct loading and asymmetric layout is given by Polit et al. [19]. In each case the structures are designed so that the maximum displacements do not involve axial stiffening in the beams.

### 2.2. Shape selection of new stage

The basic concept for the structural element of the new positioning stage is shown in Fig. 4. It adopts the direct-loaded and symmetric layout of Schitter et al. [15] because of the high stiffness of the concept. However there is an additional ‘undercut’ added to increase the length of the primary beams. The increase in length means that the beam thickness can be increased which improves out-of-plane stiffness.

The outside geometry of the structural element is determined by the clamping points, the side clamps and piezo actuators. In addition, the stage must have a means for holding a central dish. However, there is freedom to change and optimise the shape of the stage between the dish interface and the outside constraints. The main internal features can be divided into three areas:

#### 2.2.1. Primary flexural beams

The primary flexural beams are maximised in length to minimise stresses during deformation.

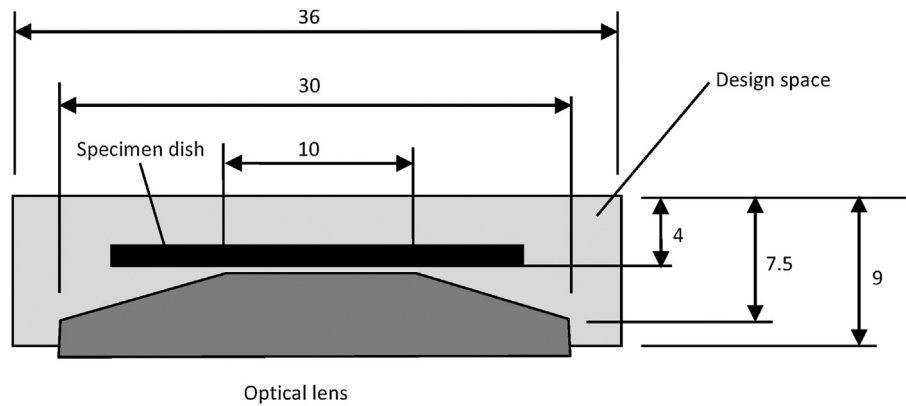
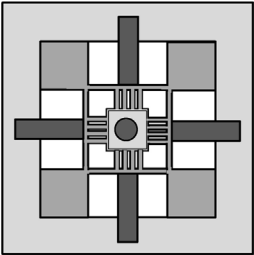
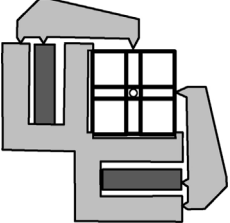
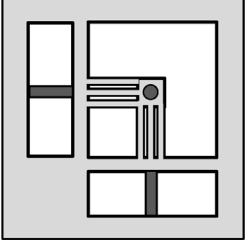


Fig. 3. Design space for the central dish holder, also showing the optical lens (part of the laser optical detection system) underneath the specimen dish.

Table 1  
Main types of positioning stage geometries.

Concept	Features
	<ul style="list-style-type: none"><li>• Symmetrical comb-flexures</li><li>• Direct and symmetrical loading</li></ul> <p>The push-pull motion of the actuators involves a more complex actuation but has the advantage of producing a higher preload The direct loading of the actuators onto the flexural beams results in a higher stiffness of the overall system</p>
	<ul style="list-style-type: none"><li>• Symmetrical beams</li><li>• Indirect and asymmetrical loading</li></ul> <p>The design is not space efficient and the pivot points reduce stiffness</p>
	<ul style="list-style-type: none"><li>• Asymmetrical flexures</li><li>• Direct and asymmetrical loading</li></ul> <p>The direct loading of the actuators onto the flexural beams results in a higher stiffness of the overall system The overall system is not space efficient Low out-of-plane stiffness due to the overhang of the central part</p>

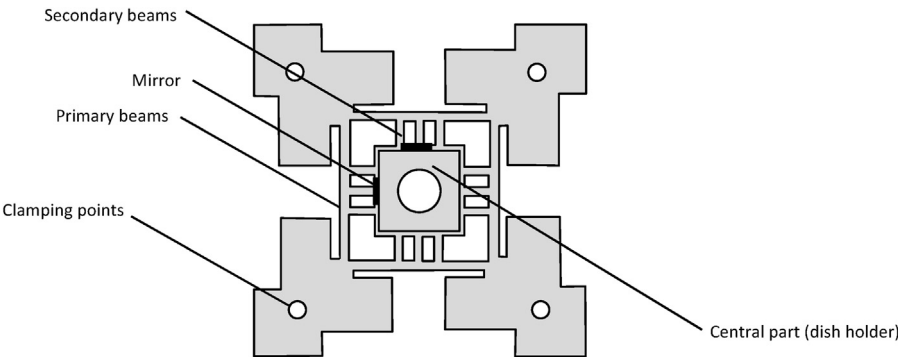


Fig. 4. Structural element of the positioning stage.

### 2.2.2. Secondary flexural beams

There are three secondary flexural beams attached perpendicularly to the primary beams. One reason for having multiple beams is that the stresses are lower for multiple beams in comparison to a single beam of the same stiffness. This is because the individual beams of a multi-beam layout are more slender (lower  $y$ ) and this leads to lower stresses because stress is a function of  $Ey/R$  where  $E$  is Young's Modulus,  $y$  is the distance to the neutral axis and  $R$  is the radius of curvature. Another advantage of multiple secondary beams is that they increase the out-of-plane stiffness of the central part of the stage by minimising the amount of overhanging sections of material. The reason for selecting three beams (and not more) was to keep manufacturing complexity down. But there would potentially be slightly higher performance from having more than three beams.

### 2.2.3. Central dish holder

The first design iterations started with a square dish holder that was not symmetrical in the  $Z$  axis. A circular shape was explored in the design optimisation as well as increased symmetry in the  $Z$  axis. The central dish holder also has two mirror holders that must be able to support mirrors for position sensing.

### 2.3. Material selection

The natural frequency of a simple spring-mass structure is given by

$$\omega = \sqrt{k/m}$$

In terms of material properties, the natural frequency of a simple spring-mass structure is a function of

$$\omega = f \left( \sqrt{E/\rho} \right)$$

Therefore the best material for achieving high frequency is the one with the highest value of  $\sqrt{E/\rho}$ .

There is an additional advantage in having a high Young's modulus because a higher modulus allows thinner sections to be made. The reason for this is that the thickness of thin sections is limited by buckling performance and buckling performance is directly proportional to the material modulus. The advantage of thinner sections is that it is possible to produce more intricate shapes that put more material away from the neutral axis thus increasing the second moment of area.

The main candidates for the position stage are steel, aluminium and titanium. Their performance is shown in Table 1, which also shows the linear thermal coefficients. Carbon Fibre Reinforced Plastic was not considered because of manufacturing limitations.

The results in Table 2 show that steel is ranked third behind titanium and aluminium for frequency. However, there is only around 8% difference between titanium and steel so the range of performance for  $\sqrt{E/\rho}$  is not that large. In terms of buckling performance, which is indicated by Young's modulus, steel is ranked first by a large margin. Therefore, steel was chosen because of its ability to form thin sections whilst still achieving a comparable frequency performance to other materials. This, is also confirmed by the fact that titanium and steel have similarly low thermal expansion coefficients, while Aluminium is more than twofold the value of titanium and steel.

### 2.4. Actuator and actuator layout selection

A schematic of the actuator layout is shown in Fig. 2. The actuators act in parallel with the structure. Piezo-actuators are a good

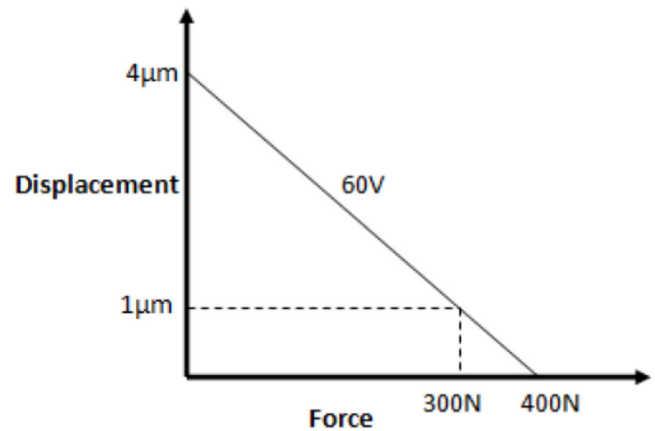


Fig. 5. Piezo actuators force to displacement relationship at 60 V.

choice for microscope positioning systems because of their high accuracy and high stiffness. Piezo-actuators were chosen that could fit into the space available whilst giving the maximum force. By maximising the actuator force this enabled the stiffness of the stage to be maximised for a given displacement. The piezo-actuators stiffness is around 18% of the stage stiffness so they add a significant amount of extra stiffness. A push-pull layout is chosen because this gives more symmetry to the displacement and enables a higher preload.

### 2.5. In-plane stiffness and preload selection

To maximise natural frequency, it is necessary to maximise in-plane stiffness. However, the stiffness is limited by the requirement for the actuators to displace the structural element by 1 μm in the  $x$  and  $y$  directions. Therefore actuators were chosen that could maximise force in the space available. The stiffness of the element was then maximised within the capabilities of the actuators.

Compressive preloads between the actuators and the structure are necessary to avoid backlash. They sum across the push-pull set-up. Hence, to compute for each actuator its own preload, for the chosen actuator arrangement (two P-885.11 actuators [20] for each direction) a blocking force of 400N needs to be considered. The maximum actuation voltage was  $\pm 60$  V and a maximum unrestricted displacement of 4 μm for the operating voltage of 60 V (Fig. 5). To displace 1 μm the maximum preload is 300N. Therefore the preload was set at 300N. This resulted in a maximum in-plane stiffness of the structural element of 600N/μm (see also documents within [20]).

This means that the structural element needed to be shaped such that the stiffness was 600N/μm in both  $x$  and  $y$  directions. Note that preloads are likely to change considering the thermal coefficient of steel (Table 1) and the piezo-actuator ( $10.8 \mu\text{m}/(\text{K m})$ ), [20] by 2.5% for a 1 K change in temperature. This should be acceptable in a closed-loop raster scan scenario and considering the good temperature stability ( $\sim 1$  K per hour) of the room for the TDFM system. A feedforward control combined with temperature sensing to adjust the preload voltage can be alternatively used.

### 2.6. Clamp selection

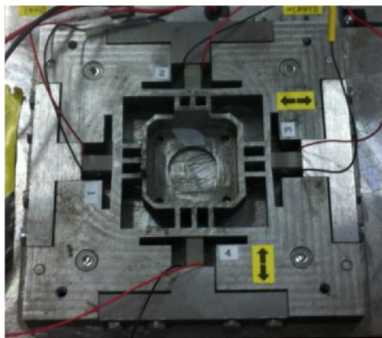
Clamping points to a rigid structure are important for achieving high frequencies. Four clamping points were chosen as shown in Fig. 4. The clamps consisted of 3 mm diameter bolts tightened with a preload of 1.5 Nm.



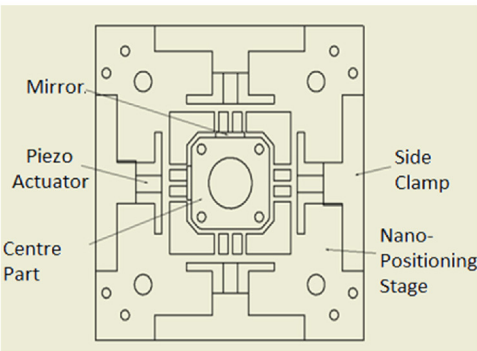
**Table 2**  
Material properties for selection of stage material.

	<i>E</i> GPa	$\rho$ kg/m <sup>3</sup>	$\sqrt{E/\rho}$	Thermal Coefficient $\alpha\mu$ m/(K m)	Rankfrequency	Rankmodulus	RankThermalExpansion
Steel	193	8080	4887	10.8	3	1	2
Aluminium	69	2710	5042	23.1	2	3	3
Titanium	114	4043	5310	8.1	1	2	1

(a) 1<sup>st</sup> HighSpeed Stage Prototype



(b) 1<sup>st</sup> High Speed Stage’s Schematic



(c) ¾ Section of the 1<sup>st</sup> High Speed Stage prototype showing z-axis assymetry

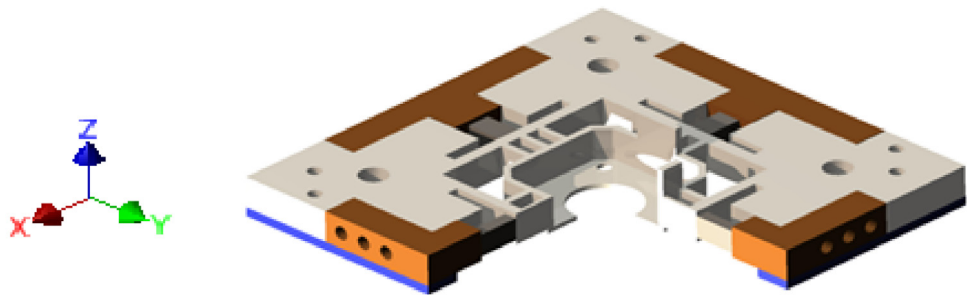


Fig. 6. High-speed-stage Prototype 1.

**3. Prototype 1 design and performance**

**3.1. Design description and rationale**

The nano-positioning stage was manufactured using stainless steel and is shown in Fig. 6. The piezo-actuators were preloaded with a 300N force through the application of 60 V and in-plane displacements were achieved through push-pull motion of the actuators.

**3.2. Testing of structural performance**

Practical Swept Sine System Identification was carried out for the first prototype, which excites the stage with sinusoidal signals at distinct frequencies within specific frequency ranges to obtain the frequency-dependent phase change and amplitude gains. A six-channel high speed piezo-drive amplifier with a voltage amplification gain of 15 ([www.techproject.at](http://www.techproject.at)) was used to drive the piezo actuators. The piezo-actuators were excited each in the X-direction and then in the Y-direction. For each excitation direction, the relevant in-plane X (or Y) translation at the flags and the ver-

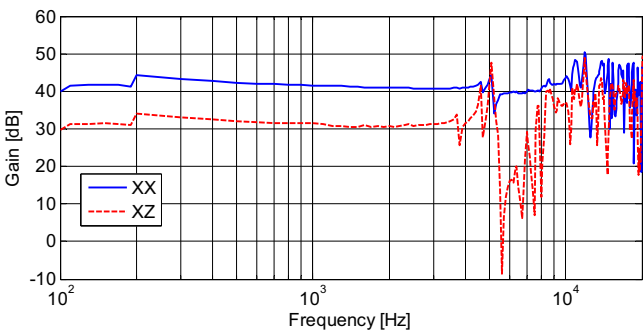
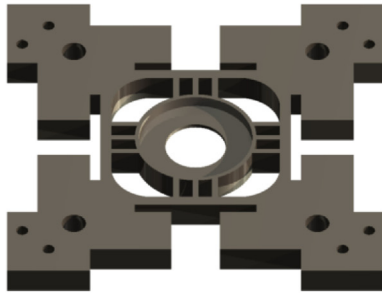


Fig. 7. Performance [nm/V] of the 1st high-speed-stage Prototype in the frequency domain using a high bandwidth piezo-amplifier with voltage gain of 15.

tical out-of-plane Z-motion at the centre part of the stage were measured. Consequently, the frequency responses were obtained, identified with XX (excitation in X-direction and translational X-direction measurement), XZ (excitation in X-direction and translational Z-direction measurement), YY or YZ (Fig. 7 for XX and XZ).

(a) Physically Idealised Model



(b) stage-centre-part with I beam cross section

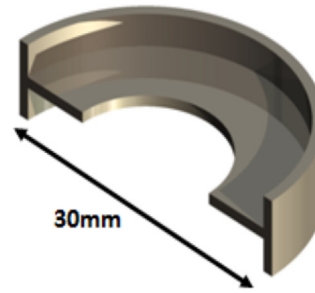


Fig. 8. Physically idealised model with the new Centre Part.

Table 3

Summary of performance of prototype 1.

	FEA	Experiment
Resonance (Hz)	7800	4500
Max out-of-plane displacements ( $\mu\text{m}$ ) for 1 $\mu\text{m}$ in plane motion	>1	0.3 (below resonance frequency)

It should be noted that in computer modelling and physical testing there is no specimen dish in the stage. The dish is very thin (0.16 mm) weighing around just 0.1 g which is typically less than 0.5% of the flexible part of the stage mass and has no significant effect on the performance.

The performance of the first prototype is summarised in Table 3.

Even though this stage achieved a high first resonance frequency of  $\sim 7.8$  kHz, Prototype 1 generated a significant amount of out-of-plane vibrations in the Z direction once actuated in-plane. Fig. 7 presents the amplifier input to translational output frequency Bode-plot derived from a swept sine analysis. It can be clearly seen that there is a difference between the in-plane and the out-of-plane motion of  $\sim 10$  dB in low frequency which provides an equivalent relative gain factor of  $\sim 3.16$  between the XX and XZ amplitude plot. Both the experimental and the FEA performance are not acceptable. The FEA out-of-plane vibrations present the worst case performance and are of similar magnitude as the desired in plane motion of 1  $\mu\text{m}$ , while the experimental results focus on the performance below the resonance, assuming that a closed-loop control strategy will not excite the high frequency resonances.

### 3.3. Lessons from prototype 1

Even though the Prototype 1 stage obtains a resonance of over 7 kHz during the Modal Analysis, and  $\sim 5$  kHz during the actual sine sweep analysis, the operational bandwidth of the high-speed-stage is restricted to 2 kHz. This is due to the significant effect of the out-of-plane vibrations beyond this frequency. The lack of symmetry of prototype 1 across the X-Y plane in the dish holder inevitably causes out-of-plane distortions during x and y movements. Therefore, it was concluded that the next prototype should be designed with vertical symmetry. In addition, it was concluded that significant shape optimisation was required to meet the performance targets.

## 4. Prototype 2 design and performance

### 4.1. Physically idealised model and design development

A new positioning-stage structure layout was developed using CAD and FEM. A CAD model was created for prototype 1 and correlated with test results to verify the validity of the model. This

Table 4

FEA predicted performance of the physically-idealised-model.

Resonance (kHz)	10,000
Max out-of-plane displacements ( $\mu\text{m}$ ) for 1 $\mu\text{m}$ in plane motion (FEA with intentionally introduced asymmetry of Piezo-actuator placement)	0.453
% increase of resonance	28%
% reduction of out-of-plane displacements	>55%

model was then used to test the effect of changes in structural shape on performance. Shape optimisation was carried out in two areas: (i) shape optimisation of the central dish holder; and (ii) shape optimization of the primary and secondary flexural beams.

### 4.2. Shape optimisation of the central dish holder

The first change in shape introduced was to replace the square central dish holder with a circular central dish holder. In addition, the asymmetry in the Z axis was replaced with a symmetric cross section in the z axis as shown in Fig. 8. The dimensions were adjusted so as to give the required in-plane stiffness of 600 N/ $\mu\text{m}$ .

The FEA of the physically-idealised-model was tested for its maximum piezo-actuator loading of 600N. The physically-idealised model demonstrated superior performance over the old high-speed-stage especially in terms of its resonance and out-of-plane displacements (Table 4). As the design assumes perfect symmetry of the physically idealised model, a vertical relative displacement of 1 mm for the piezo-actuators is deliberately introduced for all following FEAs. This induces out-of-plane motion, which otherwise would not be observed in this design.

During the FEA, it was discovered that the centre part of both the old and the new high-speed stage deformed due to the piezo-actuator loading. This is undesirable because it can cause the specimen dish to slide over the centre part surface which itself brings errors into position measurements. Hence, it was necessary to strengthen the structure of the stage-centre-part in order to minimise deformations during actuation.

### 4.3. Shape optimisation of the central part dimensions

The phenomenon of a deformed stage-centre-part was further tested with FEA. When increasing the differential actuator force to 600N, in the push-pull arrangement, there should be an overall displacement of 1  $\mu\text{m}$  displacement of the centre of the dish with deformation between the two sides of the central part having a relative displacement of zero. However, when the preloaded stage was actuated to a differential force of 600 N, the predicted relative deformation was up to 0.841  $\mu\text{m}$ . This modelling confirmed the need to stiffen the centre stage part.



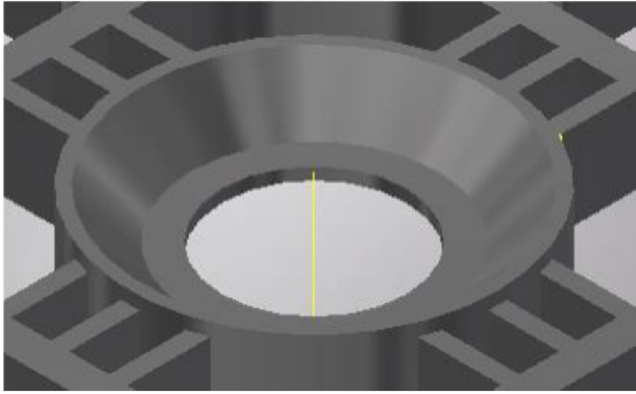


Fig. 9. Showing the 45° chamfer added to the circular ring.

Increasing the thickness of the base plate from 1 mm to 3 mm significantly reduced the deformation but also increased the mass of the stage-centre-part, and reduced the resonance bandwidth from 10 to 8.5 kHz. This thickness was chosen and the reduction of resonance was considered as an acceptable trade-off for the elimination of the measurement error.

Because the circular rim of the central part was only 1 mm in thickness it was another key source of the relative deformation. Therefore a 45° chamfer was added as shown in Fig. 9 to increase the stiffness. This further change effectively removed the relative deformation but reduced the resonance by ~1 kHz. However, this again was considered an acceptable trade-off.

#### 4.4. Shape optimisation of the primary and secondary beams

The chosen shape parameters of the primary and secondary flexural beams were  $T$ ,  $G$ ,  $W$  and  $L$ , as shown in Figs. 10(a) and (b). Their dimensions were varied in a manual iterative process, whilst maintaining the constant in-plane stiffness of ~600 N/μm.

It was observed that increasing the Gap  $W$  and  $L$  from their initial values of 2.5 mm and 22 mm respectively decreased the in-plane stiffness of the high-speed-stage. During optimization,  $W$  was maintained at its initial value, and  $L$  was increased to 25 mm in order to obtain an optimum in-plane stiffness of around 600 N/μm. Stiffness increases due to increasing  $G$  were compensated for by decreasing  $T$ .

Fig. 11 demonstrates the variation of the resonance with Gap  $G$  while its stiffness is being compensated by combined changes of  $W$  and  $T$ . From these results, the optimum length of  $G$  was increased to 6 mm, as the gradient of the curve is almost zero while its respective value for  $T$  was fixed at 1.87 mm. This decision was further supported by the requirement of having the value of  $T$  greater than 1.5 mm to provide enough structural spacing for the piezo-

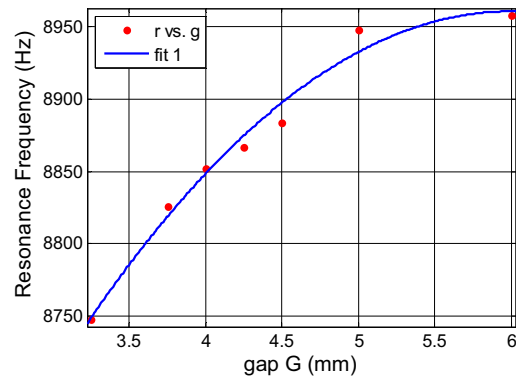


Fig. 11. Resonance variation vs. gap  $G$ , keeping gap  $L$  constant.

actuator-flexure boundary thereby preventing yielding. In fact, a minimum safety factor of 4 was maintained during this design process. These new dimensions increased the resonance from ~8.7 kHz to ~8.95 kHz.

#### 4.5. Shape optimisation- centre part re-design to fit the TDFM system

The stage-centre-part required some further re-adjustment in order for it to fit the actual optical TDFM setup. This is to avoid the surface of the optical lens (below the stage-centre-part) being in contact with the specimen dish. Perfect symmetry and chamfer profiles as shown in Fig. 12 were maintained. Overall, the stage-centre-part diameter was increased from 30 mm to 36 mm.

The modified stage-centre-part can accommodate 18 mm diameter circular specimen slides for operation. The new high-speed-stage flexure lengths were maintained, and its in-plane stiffness was tuned to approximately 600 N/μm by increasing  $L$  to 26 mm.

This stage-centre-part enlargement further decreased the resonance from ~8.9 kHz to ~7.3 kHz. A maximum out-of-plane displacement of 0.41 μm was measured in FEA with a piezo-actuator misalignment as mentioned in Section 4.1 for a maximum 600 N Piezo actuation.

A raised corrugated profile was tested on the high-speed-stage near the four bolt holes at the corners of the stage as seen in Fig. 13a. This change increased the resonance frequency from 7.3 kHz to 7.65 kHz and  $L$  was increased to 26.5 mm to retune the stiffness. This further reduced the out-of-plane displacements to 0.31 μm in the FEA. This profile also acts as a bottom supporting mount/foot profile. It reduces the contact area for the high-speed-stage to sit on the slow micro-positioning stage of the TDFM. The use of the profile will be further discussed in Section 5.2.

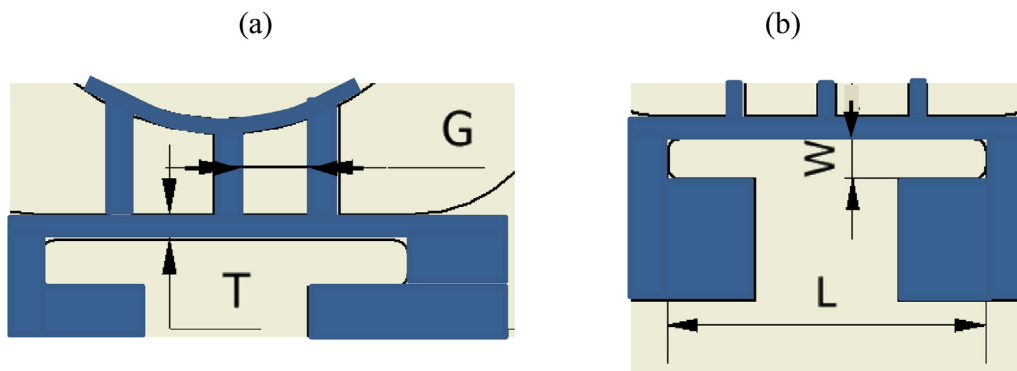
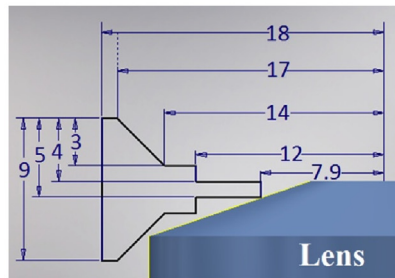


Fig. 10. Identified features to tune the stiffness.

(a) Stage-centre-part re-design



(b) New stage-centre-part cross section

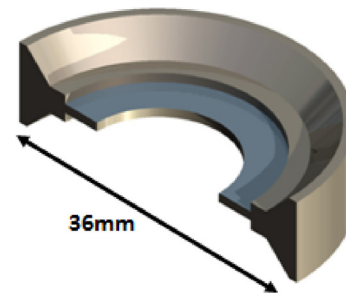
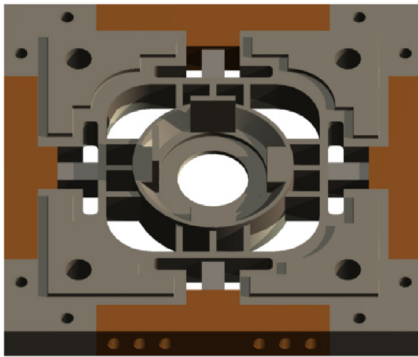
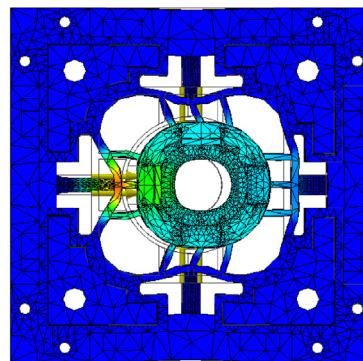


Fig. 12. Re-design of the new centre part.

(a) New high-speed-stage



(b) Single Axis Actuation



(c) Dual Axis Actuation

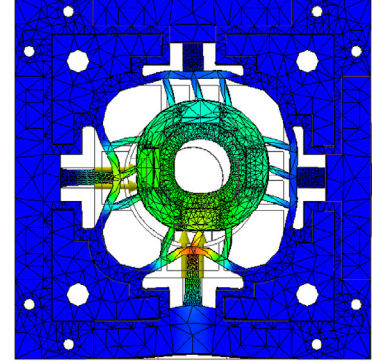
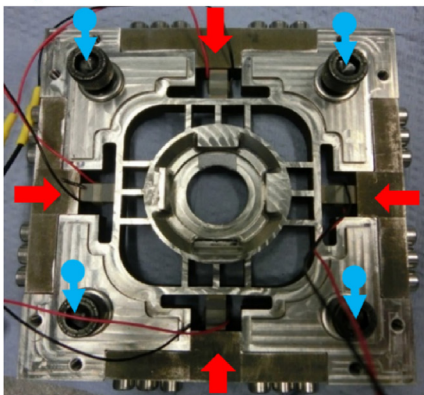


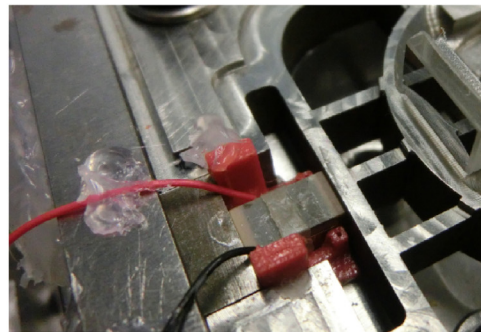
Fig. 13. New high-speed-stage design and its FEA.

(a) New high-speed-stage

(↓ = side preload)  
(⬇ = vertical preload)



(b) Piezo actuator alignment with aligner



(c) Piezo actuator aligner

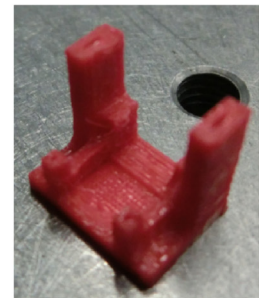


Fig. 14. Manufactured high speed nano positioning stage and piezo actuator alignment.

#### 4.5.1. Two mirrors for position measurement

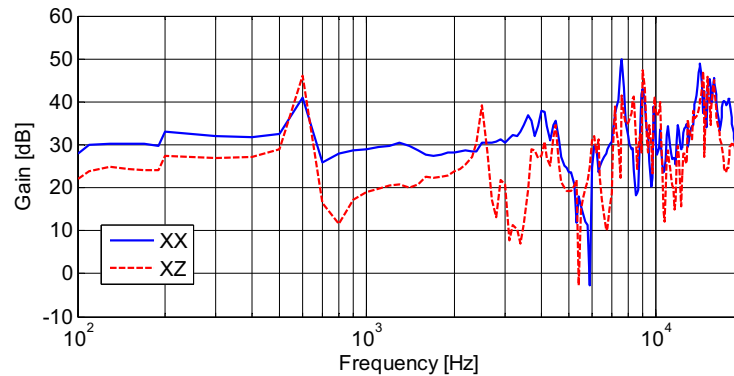
In order for the laser to detect the high-speed-stage displacements, it is required to have two mirror holding flags on the stage centre-part. They are to be kept as close to the centre as possible, while also accommodating room for the specimen slide. This is mainly to reduce the measurement error based on the difference in displacements of the specimen slide and the mirror-holding flag. In order to reduce the complexity of the milling process during manufacture of the flags, 4 rectangular profiles were added to the

stage-centre part which also supports the flags while maintaining symmetry across the XZ and YZ planes. The mirror holding flags were found to be rigid through the frequency bands of interest.

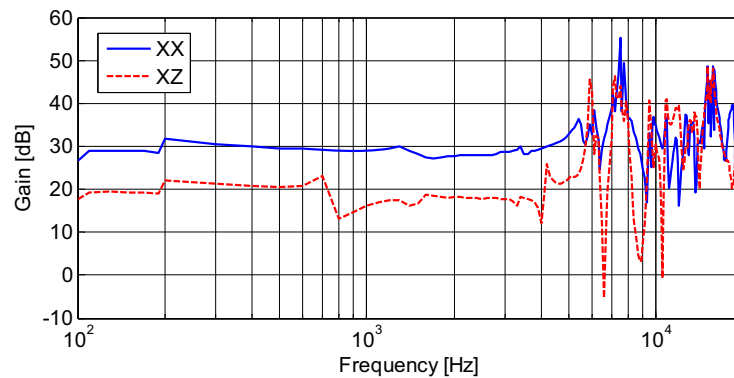
#### 4.6. Evaluation of the CAD model

The performance of the new high-speed-stage as observed in FEA (Fig. 13) is shown in Table 5. Again the same asymmetry in the piezo-actuator placement is used as for the result of Table 3.

(a) Condition A: Low vertical &amp; high side-clamp preloads



(b) Condition B: High vertical and high side-clamp preloads

**Fig. 15.** Initial high-speed-stage performance [nm/V] for different preload conditions using a high bandwidth piezo-amplifier with voltage gain of 15.**Table 5**  
FEA predicted performance of the new high-speed-stage.

Resonance (kHz)	7140
Max out-of-plane displacements ( $\mu\text{m}$ ) (FEA with intentionally introduced asymmetry of Piezo-actuator placement)	0.38
% increase of resonance	–8.5%
% reduction of out-of-plane displacements	>62%

## 5. Prototype 2 dynamic tests

### 5.1. Initial test results

After manufacture of the prototype 2 stage (Fig. 14), the frequency based system identification (as in Section 3.1) was carried out for the high-speed-stage. The high-speed-stage was first tested on a steel block mimicking the operation of the actual TDFM with bolts.

Initial test results revealed sensitivity to preload conditions as shown in Fig. 15. In addition, the best preload conditions had a performance far inferior to that predicted by FEM.

The preloads were produced and measured by use of a digital torque wrench with a 0.5–5 Nm range. The bolts were gradually tightened in sequence so that the pressure was built up uniformly over the whole stage. Initially, the best performance was observed with condition B where both the side clamp and vertical bolt preloads were high. The resonance was observed at a frequency of  $\sim 6$  kHz and the maximum out-of-plane displacement was  $0.3 \mu\text{m}$  ( $\sim 10$  dB lower than its respective in-plane motion).

It can be observed that there is a significant improvement in resonance when the vertical preload torque was increased from 0.5 to 2 Nm. This is mainly because it increased the vertical stiffness, thereby firmly holding the high-speed-stage to the base. But still the out-of-plane movements are considerably higher than predicted with the FEA model.

### 5.2. Possible causes for decreased performance of physical prototype

#### 5.2.1. Uneven bottom surface

It was suspected that the high-speed-stage bottom foot profile surface was not sufficiently flat (Fig. 16) and that this was introducing unwanted compliance into the system. In order to investigate this possibility, a thin film of red ink was coated to the bottom foot profile of the high-speed-stage and its footprint was taken on a white sheet of paper.

As seen in Fig. 17, the four foot profiles of the high-speed-stage are not level with each other. The no. 3 foot profile is clearly flatter than the rest of the profiles. The no. 4 foot profile has least contact with the paper. Therefore, the high-speed-stage tends to vibrate around its contact points when the vertical preloads are low. A lack of flatness of the positioning stage causes bending moments to be generated during preloading and these cause unwanted distortions.

#### 5.2.2. Misalignment of the piezo actuators

Another major reason for higher out-of-plane displacements is due to misalignments of the actuating piezo-actuators as these misalignments degrade the symmetry of the high-speed-stage. There

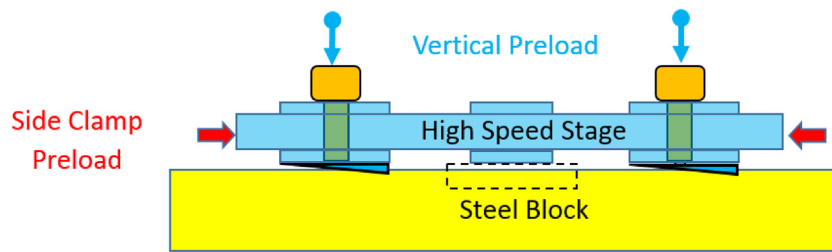


Fig. 16. Schematic of the high-speed-stage test system.

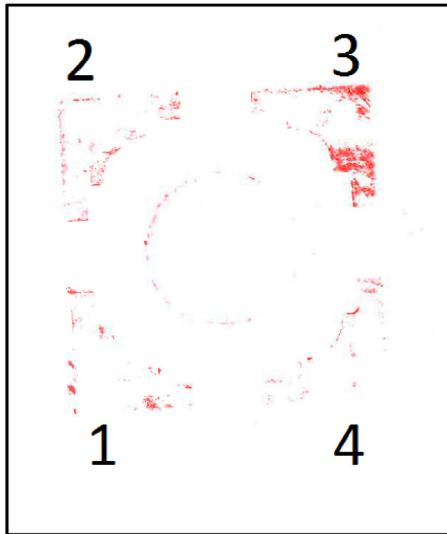


Fig. 17. Unlevelled footprints of the high-speed-stage.

was also gradual misalignment of the piezo-actuators with successive actuation. This has been observed although the side clamp preloads were controlled. The use of the piezo actuator also causes the side clamps to vibrate so that the bolts loosen. Therefore, these loose bolts may have to be retightened for each successive test.

### 5.3. Counter measures to improve on initial tests

#### Levelling of the bottom foot profiles

Two options were considered for solving the flatness problem. One was to create a three-point kinematic interface and a second was to carry out a careful grinding process to create an ultra-flat interface. A kinematic connection was not chosen because the stage has four-part symmetry and does not easily lend itself to a three-point connection. Therefore the ultra-flat machining solution was pursued.

After the first tests, the bottom foot profiles of the high-speed-stage were carefully ground so that the foot profiles were almost 100% flat and in level with each other. Similarly, the top surface of the steel block used for the high-speed-stage has also been ground so that the surface area of the high-speed-stage foot profiles was completely in contact with the steel block during testing.

With this surface modification, it was observed that the out-of-plane displacements in the X direction were  $\sim 35$  dB lower than the respective in-plane displacements, whereas before this surface modification the gain difference was only  $\sim 10$  dB, especially at low frequency. The gain difference for actuation in the Y direction was  $\sim 20$  dB for the relevant interaction with the Z and X axis as shown in Fig. 18 (b). This is mainly because the piezo actuators in the Y-direction are not as well aligned as the Piezo actuators in the X direction.

### 5.4. Custom alignment of the piezo actuators

It is clearly desirable to make both the X and Y dynamics as identical as possible in order to minimise interaction due to the relevant piezo-actuators. This simplifies the control problem to single-input-single-output structures for high-speed-stage operation. From the analysis of the results shown in Fig. 18, alignment of the piezo-actuators needs to be carried out. Identical piezo actuator aligners were 3D-printed.

### 5.5. Piezo actuators and side clamps fixed

In order to obtain consistent high-speed-stage performance in terms of displacements and out-of-plane vibrations, it was decided to leave piezo-actuator aligners to firmly hold the respective piezo actuators at the required position of the high-speed-stage. This prevented the piezo actuators from dislocating themselves due to gravity and successive testing. To avoid the bolts from loosening, the side clamps were tightened after the bolt preloads are set by a digital torque wrench and hot glue has been applied as shown in Fig. 19. This prevents any oscillatory movement of the side clamps.

### 5.6. Test results after modifications

The modifications mentioned in Section 5.3 were carried out on the high-speed-stage until the desired performance, as seen by the frequency plots of Fig. 20, was obtained.

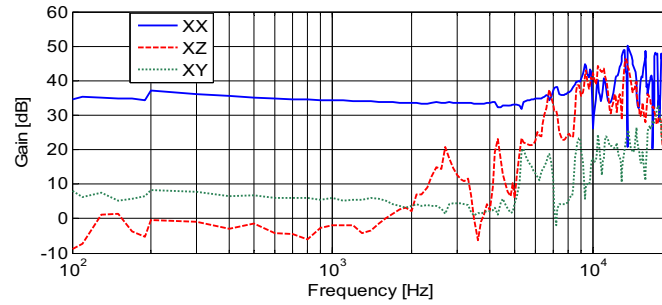
This process provides matching dynamics of both the X and Y directions. The low frequency gains of both X to X and Y to Y motion are now identical at an increased value of  $\sim 35$  dB. The gain difference for the out-of-plane displacement frequency responses in relation to their respective in-plane displacement frequency behaviour have been set to a value of larger than  $\sim 25$  dB at low frequency. Hence, for a motion of  $1 \mu\text{m}$  in-plane motion there is an out-of-plane motion of less than  $0.056 \mu\text{m}$ . This is possible because the controllers are suppressing the resonance frequency through a fast drop in controller gain at high frequency.

The out-of-plane displacements (without control) gradually increase near 6 kHz. This frequency was identified as the high-speed-stage's first resonance after all the post manufacturing modifications. This frequency is around one kHz lower than the  $\sim 7.3$  kHz observed during FEA. This is the upper bandwidth limit for the controller, which is designed in the next section.

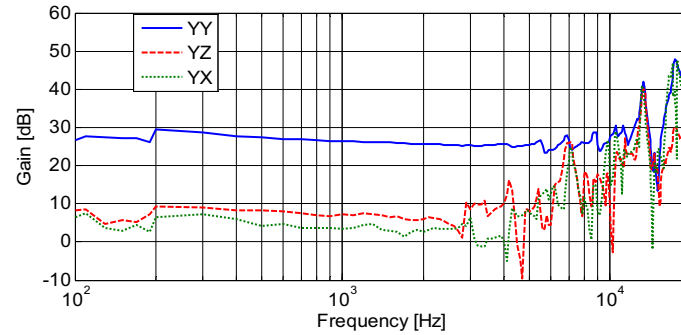
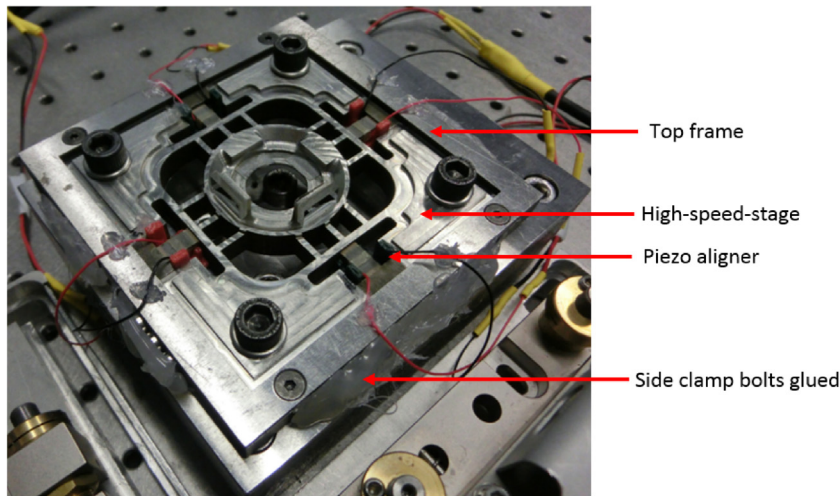
It is known that the first mode shape of a vibrating plate consists of a single peak with nodes at the restrained boundaries. This is seen by the modal analysis of the high-speed-stage during FEA. Therefore, it was understood why the out-of-plane displacements increased rapidly compared to its in-plane displacements at about 6 kHz of the actual high-speed-stage, as our point of measurement of out-of-plane displacement is at the inner edge of the centre part (the first mode shape of the high-speed-stage is shown in Fig. 21).



(a) Frequency Plot : XX, XY and XZ



(b) Frequency Plot : YY, YX and YZ

**Fig. 18.** Improved performance [nm/V] of the high-speed-stage after levelling the foot profiles.**Fig. 19.** High speed stage after all the post manufacturing modifications.

## 6. Prototype 2 closed-loop control tests

### 6.1. Controller design

The overall implementation setup and the controller design are only briefly described to retain focus on the mechanical design aspects within the limits of this paper. Fig. 22 shows the high-speed-stage system configuration (HS-NPS= High speed nano-positioning stage).

The high-speed-stage, the high-bandwidth piezo amplifier and the laser interferometer are treated as the controlled plant. The measured stage displacements in the X- and Y-axes are fed back to an FPGA based control implementation system from National Instruments (PXI-7854R) which can provide fast parallel computations and time-deterministic operation. The demanded stage positions, filters and the controllers were implemented on this

FPGA board with a sample frequency of 100 kHz. Based on the identified X and Y stage dynamics, the closed-loop controllers were designed in order to minimise the tracking errors, piezo non-linearity, disturbances and the oscillatory behaviour due to the excitations of the stage resonances at  $\sim 6.5$  kHz and  $\sim 9$  kHz. The open-loop frequency response which includes the stage and the controller dynamics in the X-axis is plotted in Fig. 23.

The frequency-shaped controller is of 4th order so that it does not consume the space of the FPGA. The gain and phase margins (Gain margin and Phase margin) of this open-loop system are 8.61 dB and  $65.3^\circ$ , respectively. Hence this guarantees a robust and stable closed-loop system. Note that the controller for the Y-axis was designed in a similar manner and so the corresponding bode plot is omitted for the sake of brevity.

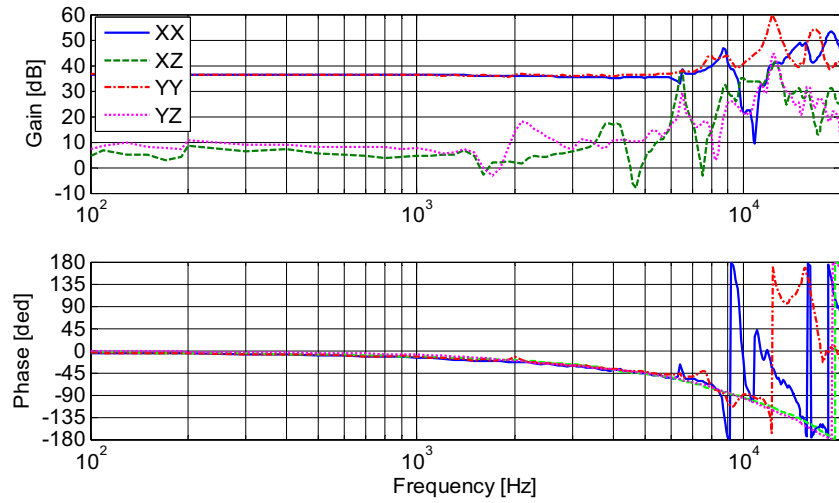
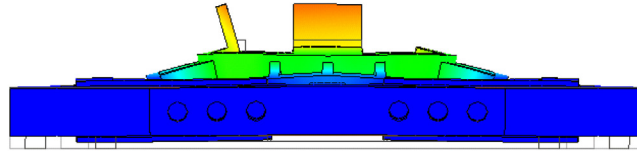


Fig. 20. Performance [nm/V] of the high-speed-stage upon post manufacturing optimisation.

(a) Side view of the high-speed-stage's first mode shape



(b) High-speed-stage's first mode shape

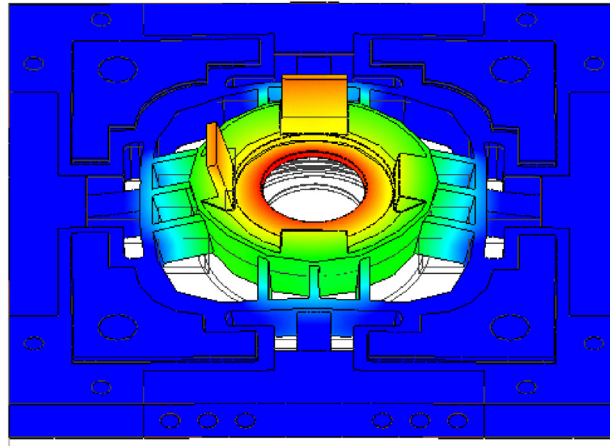


Fig. 21. First mode of the high-speed-stage as seen during FEA.

## 6.2. Comparative implementation tests results

To verify the performance of the designed controller, comparative benchmark tests (i.e. with and without the controller) were carried out. The time-series data in the X-axis of the high-speed-stage are shown in Fig. 24. The blue dashed-line is the demanded position signal, the green dash-dotted line provides the results for an open-loop configuration (i.e. without control) and the red solid-line is the result for closed-loop (i.e. with the controller) responses. As seen from Fig. 24(a), large overshoots, steady-state errors and oscillatory responses were observed for the stage without the controller. Furthermore, its response also drifts due to the piezo hysteresis. This can cause a distorted scanned image.

On the other hand, with the controller, stable and accurate tracking were maintained without the drift issue. In addition, a settling

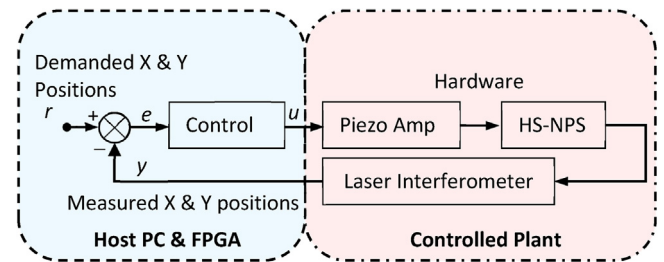
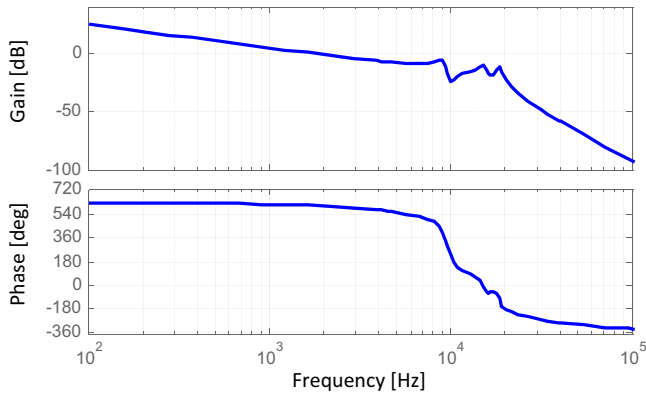


Fig. 22. Control loop structure.

time of  $\sim 0.4$  ms was achieved. Fig. 24(b) shows the test result for a triangular wave demand at 500 Hz. The open-loop controller does not work well due to the piezo drift, however the closed-loop strat-

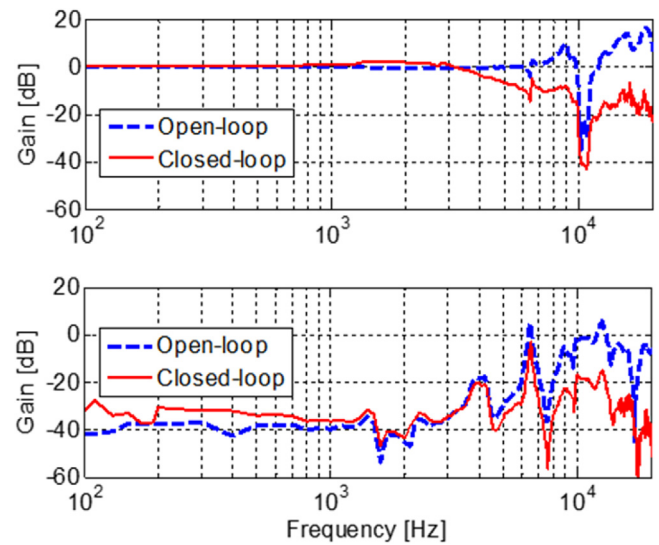




**Fig. 23.** Open-loop dynamics in the X-axis. Gain margin: 8.61 dB at 5.83 kHz, Phase margin: 65.3 deg at 1.73 kHz.

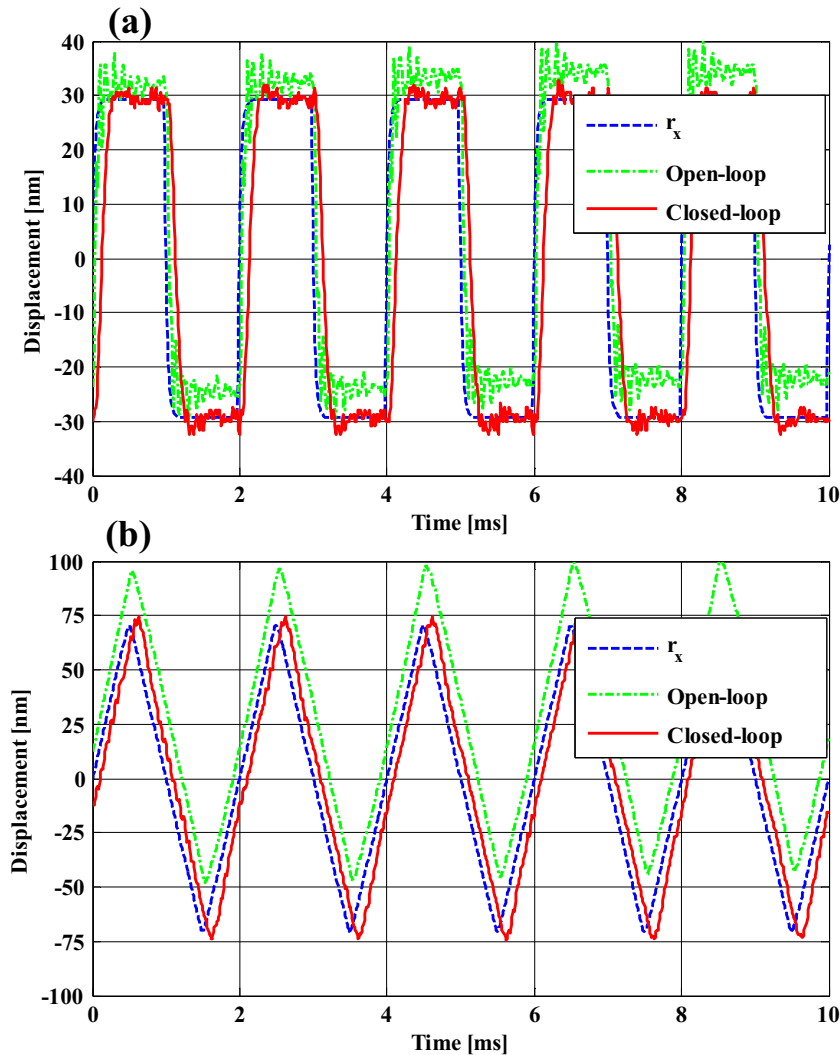
egy shows a satisfactory demand signal following performance. The frequency responses of the in-plane (XX) and the out-of-plane (XZ) dynamics with/without the controller are also presented in Fig. 25.

The stage resonances at  $\sim 6.5$  kHz and  $\sim 9$  kHz are successfully compensated by the controller. The controller is a single input single output controller that acts as a low-pass filter, suppressing the resonances. In this case, a closed-loop bandwidth of  $\sim 2$  kHz has been obtained. Moreover, noticeable out-of-plane dynamics in the



**Fig. 25.** The in-plane (XX-dynamics) and the out-of-plane (XZ-dynamics) responses in the frequency domain.

high-frequency region are also reduced. Thus, the high-speed-stage together with this controller can achieve precise high-speed scanning. Note that the Y-axis test data are omitted in this paper since



**Fig. 24.** Positioning performance with and without control: (a) Square wave (b) Triangular wave tests.

the results in the Y-axis are similar to those of the X-axis due to the symmetric structure of the high-speed-stage.

## 7. Conclusions

A bespoke high-speed positioning stage has been designed for a transverse dynamic force microscope (TDFM). An overall resonance frequency of over 6 kHz was achieved allowing a closed loop-control frequency of 1.73 kHz for precise horizontal motion control. This resonance represented a 12-fold increase from the original 500 Hz. The experimental out-of-plane distortions were reduced from 0.3  $\mu\text{m}$  to 0.05  $\mu\text{m}$ . This level of performance gives good levels of accuracy and scan speeds for the TDFM. The scanning speed is approximately 150  $\mu\text{m/s}$ .

As with most optimisation studies some key trade-offs were identified and resolved. One key trade-off involved the stiffness of the central dish holder. This part had to be stiff enough to prevent sliding of the dish but not so bulky that the overall resonance was too high. Another key trade-off involved achieving the right balance between high frequency and low-out-of plane distortions.

FEM modelling speeded up the optimisation process by revealing the relative effects of minor design changes. Practical testing proved to be essential because it identified problems that could not have been found in FEM modelling alone. In particular, practical testing revealed a lack of flatness in the bolted interface and also misalignment of the actuators.

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